Competition for Medical Supplies Under Stochastic Demand in the Covid-19 Pandemic: A Generalized Nash Equilibrium Framework

Anna Nagurney¹, Mojtaba Salarpour¹, June Dong², and Pritha Dutta³

Department of Operations and Information Management Isenberg School of Management University of Massachusetts Amherst, Massachusetts

² Department of Marketing & Management
School of Business, State University of New York, Oswego, New York

³ Department of Management and Management Science Lubin School of Business
Pace University, New York

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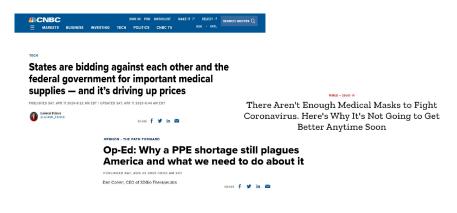
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With the Covid-19 pandemic, supply chains, including those for medical items, have been disrupted adding to the intense competition for such supplies.



The great need for medical items from Personal Protective Equipment (PPEs) to ventilators and, now, even convalescent plasma, has led to intense competition for medical supplies among healthcare institutions and even regions, including states, as well as nations.

Coronavirus USA: Federal fix sought for 'Wild West' COVID-19 PPE competition



Why Can't America Make Enough N95 Masks? 6 Months Into Pandemic, Shortages Persist

September 17, 2020 - 5:01 AM E

In Scramble for Coronavirus Supplies, Rich Countries Push Poor Aside

Developing nations in Latin America and Africa cannot find enough materials and equipment to test for coronavirus, partly because the United States and Europe are outspending them.



- China has historically produced half of the world's face masks, but with the coronavirus originating in Wuhan, China, the country dedicated the majority of the supply for their own citizens.
- Countries, such as Germany, even banned the export of PPEs.
- The intense competition for PPEs led to a dramatic increase in the price.
- The price of N95 masks grew from \$0.38 to \$5.75 each (a 1,413% increase) (Diaz, Sands, and Alesci (2020) and Berklan (2020)).
- Isolation protective gowns experienced a price increase from \$0.25 to \$5.00 (a 1900% increase).
- The price of reusable face shields went from \$0.50 to \$4.00 (a 700% increase).

- We develop a competitive game theory network model for medical supplies inspired by the Covid-19 pandemic.
- It features salient characteristics of the realities of this pandemic in terms of competition among organizations/institutions for supplies under limited capacities globally as well as uncertain demands.
- Our model includes general transportation costs.
- Since organizations, notably, healthcare ones, compete with one another for the limited supplies, given the prices and their associated logistical costs as well as the expected loss due to possible shortages or surpluses, the model is a Generalized Nash Equilibrium (GNE) model.
- In the case of GNE models not only do the objective functions of the players in the game depend on the strategies of the other players but the feasible sets do as well.

Literature Review

- The first stochastic GNE model for disaster relief was constructed by Nagurney et al. (2020).
- The constructs that we utilize for handling the uncertain demands for medical items are based on results of Dong, Zhang, and Nagurney (2004), Nagurney, Yu, and Qiang (2011) and Nagurney, Masoumi, and Yu (2012, 2015).
- Mete and Zabinsky (2010) introduced a two-stage stochastic optimization model for storage and distribution of medical supplies but considered a single decision-maker.

The network consists of m supply locations for the medical supplies, with a typical supply point denoted by i, and n locations that are demand points, with a typical demand point denoted by j.

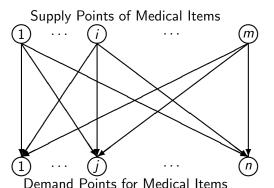


Figure: The Network Structure of the Competitive Game Theory Model for Medical Supplies

Table 1: Notation for the Medical Supply Generalized Nash Equilibrium Network Model

Definition
the amount of the medical item purchased from supply location i by j .
We first group all the i elements $\{q_{ij}\}$ into the vector q_j and then we
group such vectors for all j into the vector $q \in \mathbb{R}^{mn}_+$.
the projected demand at demand point j ; $j = 1,, n$.
the actual (uncertain) demand for the medical item at demand location
$j; j = 1, \ldots, n.$
the amount of shortage of the medical item at demand point j ; $j =$
$1,\ldots,n$.
the amount of surplus of the medical item at demand point j ; $j =$
$1,\ldots,n$.
the unit penalty associated with a shortage of the the medical item at
demand point $j; j = 1, \ldots, n$.
the unit penalty associated with a surplus of the medical item at demand
point j ; $j = 1, \ldots, n$.
the price of the medical item at supply location i ; $i = 1,, m$.
the generalized cost of transportation associated with transporting the
the medical item from supply location i to demand location j , which
includes the financial cost, any tariffs/taxes, time, and risk. We group
all the generalized costs into the vector $c(q) \in \mathbb{R}^{mn}$.
the nonnegative amount of the medical item available for purchase at
supply location $i; i = 1,, m$.
the nonnegative Lagrange multiplier associated with the supply con-
straint at supply location i . We group the Lagrange multipliers into
the vector $\mu \in \mathbb{R}^m_+$.

Stochastic Demand

Since d_j denotes the actual (uncertain) demand at destination point j, we have:

$$P_j(D_j) = P_j(d_j \leq D_j) = \int_0^{D_j} \mathcal{F}_j(t) dt, \qquad j = 1, \dots, n, \tag{1}$$

where P_j and \mathcal{F}_j denote the probability distribution function, and the probability density function of demand at point j, respectively. v_j is the "projected demand" for the medical item at demand point j; $j = 1, \ldots, n$.

Note that v_j is the "projected demand" for the medical item at demand point j; j = 1, ..., n.

Shortage and Surplus

The amounts of shortage and surplus at demand point j are calculated, respectively, according to:

$$\Delta_j^- \equiv \max\{0, d_j - v_j\}, \qquad j = 1, \dots, n, \tag{2a}$$

$$\Delta_j^+ \equiv \max\{0, v_j - d_j\}, \qquad j = 1, \dots, n. \tag{2b}$$

The expected values of shortage and surplus at each demand point are, hence:

$$E(\Delta_j^-) = \int_{v_i}^{\infty} (t - v_j) \mathcal{F}_j(t) dt, \qquad j = 1, \dots, n,$$
 (3a)

$$E(\Delta_j^+) = \int_0^{v_j} (v_j - t) \mathcal{F}_j(t) dt, \qquad j = 1, \dots, n. \tag{3b}$$

Expected Penalties

The expected penalty incurred by demand point j due to the shortage and surplus of the medical item is equal to:

$$E(\lambda_j^- \Delta_j^- + \lambda_j^+ \Delta_j^+) = \lambda_j^- E(\Delta_j^-) + \lambda_j^+ E(\Delta_j^+), \qquad j = 1, \dots, n. \quad (4)$$

Projected Demand

The projected demand at demand point j, v_j , is equal to the sum of flows of the medical item to j, that is:

$$v_j \equiv \sum_{i=1}^m q_{ij}, \qquad j = 1, \dots, n.$$
 (5)

Objective Function

The objective function of each demand point j is, hence, given by:

Minimize
$$\sum_{i=1}^{m} \rho_i q_{ij} + \sum_{i=1}^{m} c_{ij}(q) + \lambda_j^- E(\Delta_j^-) + \lambda_j^+ E(\Delta_j^+)$$
 (6)

We refer to the objective function (6) for j as the disutility of j and denote it by $DU_j(q)$; j = 1, ..., n.

Constraints

$$\sum_{i=1}^{n} q_{ij} \leq S_i, \quad i = 1, \dots, m, \tag{7}$$

$$q_{ij} \geq 0, \quad i = 1, \dots, m. \tag{8}$$

- We assume that the total generalized transportation cost functions are continuously differentiable and convex.
- In our model, the transportation costs can, in general, depend upon the vector of medical item flows since there is competition for freight service provision in the pandemic.
- In the paper, we present some preliminaries that allow us to express
 the partial derivatives of the expected total shortage and discarding
 costs of the medical items at the demand points only in terms of the
 medical item flow variables.
- We prove that the third term in the Objective Function (6) is also convex.

Feasible Set

We define the feasible sets $K_j \equiv \{q_j \geq 0\}$; j = 1, ..., n. We define $K \equiv \prod_{i=1}^{l} K_i$. We also define the feasible set $S \equiv \{q | q \text{ satisfying (7)}\}$, which consists of the shared constraints.

Definition 1: Generalized Nash Equilibrium for Medical Items

A vector of medical items $q^* \in K \cap S$ is a Generalized Nash Equilibrium if for each demand point j; j = 1, ..., n:

$$DU_{j}(q_{j}^{*}, \hat{q}_{j}^{*}) \leq DU_{j}(q_{j}, \hat{q}_{j}^{*}), \quad \forall q_{j} \in K_{j} \cap \mathcal{S}, \tag{17}$$

where $\hat{q}_{i}^{*} \equiv (q_{1}^{*}, \dots, q_{i-1}^{*}, q_{i+1}^{*}, \dots, q_{n}^{*}).$

- According to (17), an equilibrium is established if no demand point has any incentive to unilaterally change its vector of medical item purchases/shipments.
- In our model not only does the objective function of a demand point depend on the vector of strategies of its own strategies and on those of the other demand points, but the feasible set does as well.
- This model is not a Nash (1950, 1951) model, but, rather, it is a Generalized Nash Equilibrium model.
- We define the feasible set $K \equiv K \cap S$.
- Our model captures the reality of the intense competitive landscape in the Covid-19 pandemic.

Definition 2: Variational Equilibrium

A vector of medical items $q^* \in \mathcal{K}$ is a Variational Equilibrium of the above Generalized Nash Equilibrium problem if it is a solution to the following variational inequality:

$$\sum_{j=1}^{n} \sum_{i=1}^{m} \frac{\partial DU_{j}(q^{*})}{q_{ij}} \times (q_{ij} - q_{ij}^{*}) \ge 0, \quad \forall q \in \mathcal{K},$$
(18)

where $\langle \cdot, \cdot \rangle$ denotes the inner product in *mn*-dimensional Euclidean space.

In expanded form, the variational inequality in (18) is: determine $q^* \in \mathcal{K}$ such that

$$\sum_{j=1}^{n} \sum_{i=1}^{m} \left[\rho_{i} + \sum_{l=1}^{m} \frac{\partial c_{lj}(q^{*})}{\partial q_{ij}} + \lambda_{j}^{+} P_{j} \left(\sum_{l=1}^{m} q_{lj}^{*} \right) - \lambda_{j}^{-} \left(1 - P_{j} \left(\sum_{l=1}^{m} q_{lj}^{*} \right) \right) \right] \times \left[q_{ij} - q_{ij}^{*} \right] \geq 0,$$
(19)

Standard Form

From Nagurney (1999) we know that finite-dimensional variational inequality problem, $VI(F, \mathcal{K})$, is to determine a vector $X^* \in \mathcal{K} \subset R^N$, such that

$$\langle F(X^*), X - X^* \rangle \ge 0, \quad \forall X \in \mathcal{K},$$
 (20)

where F is a given continuous function from \mathcal{K} to R^N , and \mathcal{K} is a given closed, convex set.

We let $X \equiv q$ and F(X) be the vector with elements: $\{\frac{\partial DU_j(q^*)}{q_{ij}}\}$, $\forall j, i$ with \mathcal{K} as originally defined and N=mn. Then, clearly, variational inequality (19) can be put into standard form (20), under our assumptions.

We associate a nonnegative Lagrange multiplier μ_i with constraint (7), for each supply location $i=1,\ldots,m$. We group all the Lagrange multipliers into the vector $\mu\in R_+^m$. We define the feasible set $\mathcal{K}^2\equiv\{(q,\mu)|q\geq 0,\mu\geq 0\}$.

Alternative Variational Inequality

Using arguments as in Nagurney, Salarpour, and Daniele (2019), an alternative variational inequality for (19) is: determine $(q^*, \mu^*) \in \mathcal{K}^2$ such that

$$\sum_{j=1}^{n} \sum_{i=1}^{m} \left[\rho_{i} + \sum_{l=1}^{m} \frac{\partial c_{lj}(q^{*})}{\partial q_{ij}} + \lambda_{j}^{+} P_{j} \left(\sum_{l=1}^{m} q_{ij}^{*} \right) - \lambda_{j}^{-} \left(1 - P_{j} \left(\sum_{l=1}^{m} q_{ij}^{*} \right) + \mu_{i}^{*} \right) \right] \times \left[q_{ij} - q_{ij}^{*} \right]$$

$$+\sum_{i=1}^{m} \left[S_{i} - \sum_{i=1}^{n} q_{ij}^{*} \right] \times \left[\mu_{i} - \mu_{i}^{*} \right] \geq 0, \quad \forall (q, \mu) \in \mathcal{K}^{2}.$$
 (21)

- The illustrative examples are inspired by the Covid-19 pandemic and associated challenges in procuring N95 face masks.
- The supply point sells 20-pack N95 masks in the form of large bulks of 1000 packs each; therefore, one unit of item flow from the supply point to a demand point, q_{ii}, represents 1000 of 20-pack N95 masks.
- The demand at the demand point is uniformly distributed between 100 and 1,000 of large bulks.





Figure: Network Topology for Illustrative Example 1



Figure: Network Topology for Illustrative Example 2

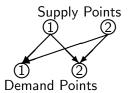


Figure: Network Topology for Illustrative Example 3

- We assume that the price of each 20-pack N95 mask during the pandemic is \$25, so that the purchase price of each large bulk is $\rho_1 = 25,000$.
- We assume that, for every 2,000 people who do not use the face mask, one person would die due to the disease.
- Although it is not easy to value people's lives, we assume a \$200,000 equivalent for each loss. As a result, the penalty, λ_1^- , on the shortage of one item flow, which is equivalent to 20,000 N95 masks, is set at \$2,000,000.
- We also consider a penalty of $\lambda_1^+=100,000$ on surplus item flows to avoid overloading.

Data for Illustrative Example 1

$$ho_1=25,000, \quad S_1=1,000, \quad c_{11}(q)=q_{11}^2+3q_{11}, \ \lambda_1^-=2,000,000, \quad \lambda_1^+=100,000.$$

We can rewrite variational inequality (21) for this example as: determine $(q^*, \mu^*) \in \mathcal{K}^2$ such that:

$$\left[25000 + 2q_{11}^* + 3 + 100000(\frac{q_{11}^* - 100}{900}) - 2000000(\frac{1000 - q_{11}^*}{900}) + \mu_1^* \right] \times [q_{11} - q_{11}^*]$$

$$+ [1000 - q_{11}^*] \times [\mu_1 - \mu_1^*] \ge 0, \quad \forall (q, \mu) \in \mathcal{K}^2$$

The solution to the above variational inequality, which we obtained analytically, is:

$$q_{11}^* = 945.62, \quad \mu_1^* = 0.00.$$

Additional Data for Illustrative Example 2

$$\rho_2 = 10,000, \quad S_2 = 500, \quad c_{21}(q) = 2q_{21}^2 + 4q_{21}.$$

Additional Data for Illustrative Example 3

The demand for the new demand point is uniformly distributed between 100 and 500. The generalized transportation cost functions and the penalty coefficients associated with the second demand point are:

$$c_{12}(q) = 2q_{12}^2 + 3q_{12}, \quad c_{22}(q) = 3q_{22}^2 + 4q_{22},$$
 $\lambda_2^- = 2,000,000, \quad \lambda_2^+ = 100,000.$

- In Example 1, the projected demand value $v_1 = 945.62$ which is very close to the upper bound.
- The disutility of the organization in this logistical operation is equal to 67.543,534.04.
- In Example 2, with the addition of a new supply point that offers lower price, the decision-makers purchase more items from supply point 2.
- The supply capacity of the new supply point is half that of the first supply point, and we see that all its capacity has been used. Therefore, the associated equilibrium Lagrange multiplier is positive.
- Now, with greater flexibility in the supply chain due to the addition of a new supply point, the disutility of the organization at the demand point has declined, dropping to 59,860,548.75.

- In Example 3, it can be seen that the full capacity of supply point 2
 has not been assigned to demand point 1, since the organization at
 demand point 1 now competed with the organization at demand
 point 2.
- The major part of the demand point 1's procurement of the N95 masks is from supply point 1 that has a larger capacity as compared to supply point 2.
- The addition of a new demand point to the competition has changed the strategies of the organization at demand point 1, and we can see the impact on its disutility. Its disutility has now increased to 62,580,546.57. The disutility of the second demand point is 28,457,845.74.

Qualitative Properties

Theorem 2: Monotonicity

The function F(X) is monotone, for all $X \in \mathcal{K}$, if all the generalized transportation cost functions c_{ij} , i = 1, ..., m; j = 1, ..., n, are convex.

Theorem 3: Uniqueness

The function F(X) is strictly monotone for all $X \in \mathcal{K}$, if all the generalized transportation cost functions c_{ij} ; $i=1,\ldots,m$; $j=1,\ldots,n$, are strictly convex. Then the variational inequality (21) has a unique solution in \mathcal{K}

Theorem 4: Lipschitz Continuity

If the generalized transportation cost functions c_{ij} , for all i and j, have bounded second order partial derivatives, then the function F(X) that enters the variational inequality problem (21) is Lipschitz continuous; that is, there exists a constant L>0, known as the Lipschitz constant, such that

$$||F(X^1) - F(X^2)|| \le L||X^1 - X^2||, \quad \forall X^1, X^2 \in \mathcal{K}.$$
 (25)

Algorithm

Modified Projection Method (Korpelevich (1977))

Step 0: Initialization

Initialize with $X^0 \in \mathcal{K}$. Set the iteration counter $\tau := 1$ and let β be a scalar such that $0 < \beta \leq \frac{1}{L}$, where L is the Lipschitz constant.

Step 1: Computation

Compute \bar{X}^{τ} by solving the variational inequality subproblem:

$$\langle \bar{X}^{\tau} + \beta F(X^{\tau-1}) - X^{\tau-1}, X - \bar{X}^{\tau} \rangle \ge 0, \quad \forall X \in \mathcal{K}.$$
 (26)

Step 2: Adaptation

Compute X^{τ} by solving the variational inequality subproblem:

$$\langle X^{\tau} + \beta F(\bar{X}^{\tau}) - X^{\tau-1}, X - X^{\tau} \rangle \ge 0, \quad \forall X \in \mathcal{K}.$$
 (27)

Step 3: Convergence Verification

If $|X^{\tau} - X^{\tau-1}| \le \epsilon$, with $\epsilon > 0$, a pre-specified tolerance, then stop; otherwise, set $\tau := \tau + 1$ and go to Step 1.

Algorithm

Explicit Formula for the Medical Item Flow

Determine $\bar{q}_{ij}^{\, au}$ for each i,j at Step 1 iteration au according to:

$$\bar{q}_{ij}^{\tau} = \max\{0, q_{ij}^{\tau-1} + \beta(-\rho_i - \sum_{l=1}^m \frac{\partial c_{lj}(q^{\tau-1})}{\partial q_{ij}} - \lambda_j^+ P_j(\sum_{l=1}^m q_{lj}^{\tau-1}) +$$

$$\lambda_{j}^{-}(1-P_{j}(\sum_{l=1}^{m}q_{lj}^{\tau-1}))-\mu_{i}^{\tau-1})\}.$$
 (28)

Explicit Formula for the Lagrange Multiplier

Determine $\bar{\mu}_i^{\tau}$ for each i at Step 1 iteration τ according to:

$$\bar{\mu}_{i}^{\tau} = \max\{0, \mu_{i}^{\tau-1} + \beta(-S_{i} + \sum_{i=1}^{n} q_{ij}^{\tau-1})\}.$$
 (29)

- The network consists of a single supply point and a single demand point.
- \bullet The q_{ij} s are in units since these medical practices are small relative to hospitals, etc.
- We assumed a uniform probability distribution in the range [100, 1000] at the demand point.
- The additional data for this example are:

$$ho_1=2, \quad S_1=1,000, \quad c_{11}(q)=.005q_{11}^2+.01q_{11}, \ \lambda_1^-=1,000, \quad \lambda_1^+=10.$$

• The computed equilibrium solution is:

$$q_{11}^* = 980.56, \quad \mu_1^* = 0.00.$$

• The projected demand of 980.56 is close to the upper bound of the probability distribution at the demand point.

- There is one supply point and two demand points.
- This example has the same data as Numerical Example 1 except for the following additional data for the new demand point:

$$c_{12}(q) = .01q_{12}^2 + .02, \quad \lambda_2^- = 1000, \quad \lambda_2^+ = 10.$$

 The modified projection method converged to the following equilibrium solution:

$$q_{11}^* = 502.20, \quad q_{12}^* = 497.80, \quad \mu_1^* = 541.61.$$

• The available supply of 1,000 N95 masks is exhausted between the two demand points, and, hence, the associated Lagrange multiplier μ_1^* is positive.

- The network consists of two supply points and two demand points.
- The data are same as that of Example 2 with the following additions:

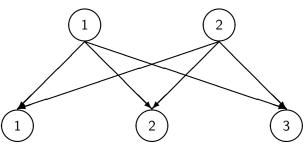
$$S_2 = 500$$
, $\rho_2 = 3$, $c_{21}(q) = .015q_{21}^2 + .03$, $c_{22}(q) = .02q_{22}^2 + .04q_{22}$.

The modified projection method yielded the following equilibrium solution:

$$q_{11}^*=526.31, \quad q_{12}^*=473.69, \quad q_{21}^*=225.57,$$
 $q_{22}^*=274.43, \quad \mu_1^*=261.17, \quad \mu_2^*=258.65.$

The network consists of two supply points and three demand points.





Demand Points

Figure: Network Topology for Numerical Example 4

 Numerical Example 4 has the same data as Numerical Example 3 but with the addition of data for demand point 3 as follows:

$$c_{13}(q) = .01q_{13}^2 + .02q_{13}, \quad c_{23}(q) = .015q_{23}^2 + .03q_{23},$$
 $\lambda_3^- = 1000, \quad \lambda_3^+ = 10.$

- The probability distribution for the N95 masks associated with demand point 3 is uniform with a lower bound of 200 and an upper bound of 1000.
- The modified projection method yielded the following equilibrium solution:

$$q_{11}^*=360.11, \quad q_{12}^*=318.83, \quad q_{13}^*=321.06,$$
 $q_{21}^*=122.29, \quad q_{22}^*=161.10, \quad q_{23}^*=216.62,$ $\mu_1^*=565.25, \quad \mu_2^*=564.16.$

There are two supply points and four demand points.

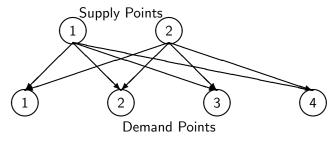


Figure: Network Topology for Numerical Example 5

Additional data for the new demand point 4:

$$c_{14}(q)=.015q_{14}^2+.03q_{14}, \quad c_{24}(q)=.025q_{24}^2+.05q_{24}, \ \lambda_4^-=1000, \quad \lambda_4^+=10.$$

 The modified projection method now yielded the following equilibrium solution:

$$q_{11}^*=260.73, \quad q_{12}^*=229.36, \quad q_{13}^*=251.22, \quad q_{14}^*=258.69,$$

$$q_{21}^*=79.57, \quad q_{22}^*=109.17, \quad q_{23}^*=160.46,$$

$$q_{24}^*=150.81, \quad \mu_1^*=725.71, \quad \mu_2^*=724.91.$$

Summary and Conclusions

- In Numerical Example 2 we see that with increased competition for N95 mask supplies from the second demand point, the first demand point has a large reduction in procured supplies, as compared to the volume received in Numerical Example 1.
- With the addition of a new supply point in Numerical Example 3, both demand points gain significantly in terms of the volume of N95 that each procures and the supplies at each supply point are fully sold out.
- In Numerical Example 4 with increasing competition for the N95 masks with another demand point, both demand points 1 and 2 experience decreases in procurement of supplies. The two supply points again fully sell out of their N95 masks.
- In Numerical Example 5 the suppliers of the N95 sell out their supplies. However, the demand points lose in term of supply procurement for their organizations with the increased demand and competition from and yet another demand point.

Summary and Conclusions

- Medical supplies are essential in the battle against the coronavirus that causes Covid-19.
- The demand for medical supplies globally from PPEs to ventilators has created an intense competition.
- We developed a Generalized Nash Equilibrium model that consists of multiple supply points for the medical items and multiple demand points with the demand at the latter being stochastic.
- Using some recently introduced machinery we were able to provide alternative variational inequality formulations of the equilibrium conditions.

Summary and Conclusions

- We utilized the variational inequality with not only medical item product flows as variables but also the Lagrange multipliers associated with the supply capacities of the medical items at the supply point.
- We studied the model quantitatively through illustrative examples that we
 were able to solve analytically as well as via numerical examples for which
 we utilized an algorithm that we proposed.
- The findings from the numerical examples confirm that more supply points with sufficient supplies are needed to ensure that organizations are not deprived of critical supplies due to competition.
- As a result of this competition and limited local availability; in particular in the case of supplies such as masks and even coronavirus test kits, we are seeing several countries now setting up local production sites.
- This model can be applied to study the network economics of a spectrum of medical items, both in the near term, and in the longer term, as when vaccines as well as medicines for Covid-19 become available.

Acknowledgement

This work is dedicated to all essential workers, including: healthcare workers, first responders, freight service providers, grocery store workers, farmers, and educators, who sacrificed so much in the Covid-19 pandemic.



Thank you!